## Announcements 23 Mar 09

- Online homework \#6 due on Wed by 8 am
- Problem 5.22 Part A:
give your answer with only 2 significant digits!
- Homework \#7
- Written homework due on Friday in class
- Online homework due next week on Tuesday


## - Exam \#2

- Tuesday April 7 from 7 to 9 pm


## Friction

Friction occurs when two surfaces are in contact and (attempt to) slide over one another

Friction tends to prevent the two surfaces from sliding over each other

Friction is due to surfaces not being smooth

DEMOS:
sliding table
sliding brick with force gauge sliding block on inclined plane


Friction increases as the force that pushes the two surfaces against each other increases (actual surface area in contact increases)

## Static Friction



## Kinetic Friction



$$
f_{\mathrm{k}}=\mu_{k} n \quad \quad \mu_{k}=\text { coefficient of kinetic friction }
$$

| Friction and Materials |  | $\mu_{\mathrm{k}}$ | $\mu_{\mathrm{s}}$ |
| :--- | :--- | :--- | :--- |
| For nearly all materials, | Rubber on <br> concrete <br> (dry) | 0.80 | 0.90 |
| $\mu_{\mathrm{s}}>\mu_{\mathrm{k}}$ | Steel on steel | 0.57 | 0.74 |
| Static friction $>$ Kinetic friction | Glass on <br> glass | 0.40 | 0.94 |
| This is why drivers are always | Wood on <br> leather | 0.40 | 0.50 |
| Copper on <br> steel | 0.36 | 0.53 |  |
| advised to not lock their wheels <br> in emergency braking situations. | Rubber on <br> concrete | 0.25 | 0.30 |
| Car manufacturers put anti-lock <br> (wet) | Steel on ice | 0.06 | 0.10 |
| break systems (ABS) in cars <br> for this reason. | Waxed ski on <br> snow | 0.05 | 0.10 |
|  | Teflon on <br> Teflon | 0.04 | 0.04 |

## Working with Friction Forces

(1) If the object is not moving relative to the surface it's in contact with, the friction force is static friction. Draw a free-body diagram of the object. The direction of the friction force is such as to oppose sliding of the object. Then use Problem-Solving Strategy 5.1 or 5.2 to solve for $f_{\mathrm{s}}$. If $f_{\mathrm{s}}$ is greater than $f_{\mathrm{smax}}=\mu_{\mathrm{s}} n$, then static friction cannot hold the object in place. The assumption that the object is at rest is not valid, and you need to redo the problem using kinetic friction.
(2) If the object is sliding relative to the surface, then kinetic friction is acting. From Newton's second law, find the normal force $n$. Equation 5.13 then gives the magnitude and direction of the friction force.

If object is not moving relative to the surface it's in contact with: $f_{k}=0$ If object is moving relative to the surface it's in contact with: $f_{s}=0$

## Applying 2nd Law (Revisited example with friction)

A 75-kg skier starts down a $50-\mathrm{m}$ high, $10^{\circ}$ slope. The coefficients of friction between the skis and the snow are $\mu_{\mathrm{s}}=0.12$ and $\mu_{\mathrm{k}}=0.06$.
What is the skier's speed at the bottom?

How to approach this problem?

1. Identify all forces acting on the skier (and only those)

2. Determine $x$ - and y-components of the net force (using conveniently tilted $x$ - and $y$-axes)

$$
\begin{aligned}
& \Sigma F_{x}=w \sin 10^{\circ}-f_{k} \quad \Sigma F_{y}=n-w \cos 10^{\circ} \\
& \text { but } a_{y}=0 \text {, thus } \Sigma F_{y}=0 \text { and } n=w \cos 10^{\circ}
\end{aligned}
$$

3. Compute acceleration from the knowledge of the net force and Newton's 2nd law: $a_{x}=\Sigma F_{x} / m=\left[w \sin 10^{\circ}-\mu_{k}\left(w \cos 10^{\circ}\right)\right] / m$
4. Given that acceleration, use kinematics equations to determine the skier's velocity: $\left(v_{x}\right)_{f}^{2}=\left(v_{x}\right)_{i}^{2}+2 a_{x} \Delta x$

## Friction Question 1

A moving block of mass M is continuously being pulled by a rope under tension T and the speed of the block is constant. [Friction is present.] If the same tension continues to be applied but the mass of the block were to suddenly become 2 M , the block would
A. Keep moving at the same speed.
B. Move with half the speed.
C. Immediately slow down and later come to a stop.
D. None of the above.

Answer: C

$$
v=?
$$


$M \longrightarrow T$


## Friction Question 2

An automotive engineer suggests increasing the mass of a car to shorten its stopping distance, since the stopping force on a car goes as $\mu_{\mathrm{s}} \mathrm{mg}$. Would this work?
A. Yes, cool idea!
B. No way!
C. I need help to answer this...

## Friction Question 2

An automotive engineer suggests increasing the mass of a car to shorten its stopping distance, since the stopping force on a car goes as $\mu_{\mathrm{s}} \mathrm{mg}$. Would this work?

It's true that the stopping force is $\mathrm{f}_{\mathrm{s}}=\mu_{\mathrm{s}} \mathrm{n}=\mu_{\mathrm{s}} \mathrm{mg}$, however we need to consider Newton's second law $\Sigma \mathrm{F}=\mathrm{ma}$

$$
\begin{aligned}
\Sigma \mathrm{F} & =\mathrm{ma} \\
\mu_{\mathrm{s}} \mathrm{mg} & =\mathrm{ma} \\
\mu_{\mathrm{s}} \mathrm{~g} & =\mathrm{a}
\end{aligned}
$$

So the car's deceleration is independent of its mass, and the stopping distance is independent of mass
Not going to work!

## Friction Problem

A car traveling at $20 \mathrm{~m} / \mathrm{s}$ stops in a distance of 50 m . Assume that the deceleration is constant. The coefficients of friction between a passenger and the seat are $\mu_{\mathrm{s}}=0.5$ and $\mu_{\mathrm{k}}=0.3$. Will a $70-\mathrm{kg}$ passenger slide off the seat if not wearing a seat belt?

## How do we solve this problem? <br> What are we asked to find? <br> Where do we start?

We need to think about what is the force that keeps the person in the seat.

## Friction Problem

Static friction is the only horizontal force that keeps the passenger in the seat

We need to find out what is the maximum acceleration from static friction and compare that to the acceleration of the car

If the car's acceleration is greater, the person will slide and if it is less then the passenger will remain in the seat

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Max Acceleration from friction
$\sum F_{x}=m a$

Acceleration of car

$$
\left(v_{x}\right)_{f}^{2}=\left(v_{x}\right)_{i}^{2}+2 a \Delta x
$$

The Force of Gravity

## Ofif the mark by Mark Parisi



SIR ISAAC NEWTON WOULD HAVE
DISCOVERED GRAVITY YEARS EARLIER HAD WILLIAM TELL NOT WANDERED BY

Sir Isaac Newton


Is there a connection between
these two motions?
Apple falling from a tree vs. Moon orbiting Earth


