Introduction to 1D and 2D NMR Spectroscopy

(2) Vector Model and Relaxations

Lecturer: Weiguo Hu 7-1428 weiguoh@umass.edu February 2023

Rules of Electromagnetism (1): Behaviors of the Magnetic Moments

- In the field of gravity, a stationary object would simply fall, while a spinning object (a *moment*) would precess
 - Precession is around the direction of gravity
- 2. Precession of the magnetic moment on the horizontal plane (around the z-axis) emits signal
- Signal intensity ∞ amplitude of horizontal component



1

Rules of Electromagnetism (2): Resonance

- When the frequency of the pulse satisfies the Larmor Equation ("resonance"), the oscillation of the pulse and the external field B₀ cancels each other, resulting in a static horizontal magnetic field B₁
 - i.e., during pulsing, B_{0} can be considered non-existent, and only B_{1} is at play
 - B₀ and B₁ are the magnetic fields, which influence the magnetic moments
 - I is the magnetic moments, i.e., the object to be manipulated by the fields



3

Vector Model of NMR **



- 1. Magnetic moments are aligned along z direction
- A pulse creates a horizontal magnetic field B₁ along -y direction, which (1) cancels B₀; (2) causes the magnetic moments to precess around B₁

The pulse stops when the magnetic moments turns 90° , toward x

4. Magnetic moments precess around B₀, generating signal

- Two precessions:
 - $\begin{array}{ll} & 1. \mbox{ during pulsing, on a vertical circle, around the horizontal field B_1 created by the pulse} \\ & 2. \mbox{ after pulse stops, on a horizontal circle, around the vertical big field B_0} \end{array}$
- Angle turned by the pulse ∞ pulse length
- Signal strength ∞ horizontal component of the magnetic moment

Signal strength at imcrementing pulse length



- Increment step = 0.4 µs
- First maximum of signal appears at ca. 4.6 μs
- First null point appears at 9.6 μ s
- 5

Use These Questions to Familiarize Yourself with Vector Model

- Suppose a pulse of 10 µs turns the vector by 90°, generating a signal with intensity of 1. What would signal intensity be for pulses of
 - 20 μs?
 - 30 μs?
 - 40 μs?
 - 5 μs?
 - 3.33 μs?

6

T_1 and T_2 Relaxations



- Relaxation: process from high-energy (excited) state to lowenergy (equilibrium) state
- The higher the energy gain upon relaxation, the easier the relaxation is to occur

7

8

Relaxations in Vector Model **



- T_1 : coming back to $I_z = 1$ (with no concern about $I_{x,y}$)
- T₂: coming back to I_{x,y} = 0 (with no concern about I_z)
- T₁ and T₂ are independent processes
 Vertical and horizontal components recover at different rates
- Don't confuse T_1/T_2 relaxation with molecular relaxation

T₁ Measurement: Inversion Recovery



- What does the 180° pulse do?
- The 90° pulse: read out the signal



- Why should I care about T₁ and T₂?
 - Is my spectrum quantitative?
 - Is everything in my sample showing up on the spectrum?
 - What are my molecule's physical behaviors?
- T₁ relaxation time affects signal intensity –Why?
- T₂ relaxation time affects signal width

$$-\Delta \nu = \frac{1}{\pi T_2}$$

4	4
1	1

11

Important Concepts

- Nuclear magnetic moments follow the rules of classical electromagnetics
 - Magnets will "precess" in an external magnetic field
 - Only horizontal component of magnetic moments gives out signal
- A 90° pulse, a 180° pulse, and what they do
- What are T₁ and T₂ relaxations, and what NMR properties that they affect